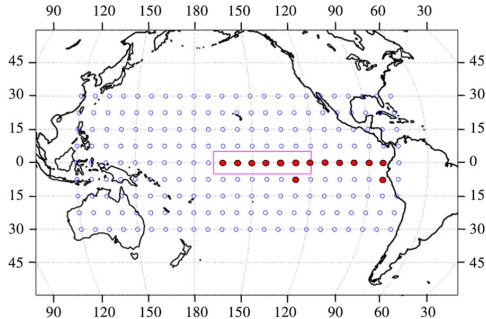


NETWORKS IN CLIMATE SCIENCE

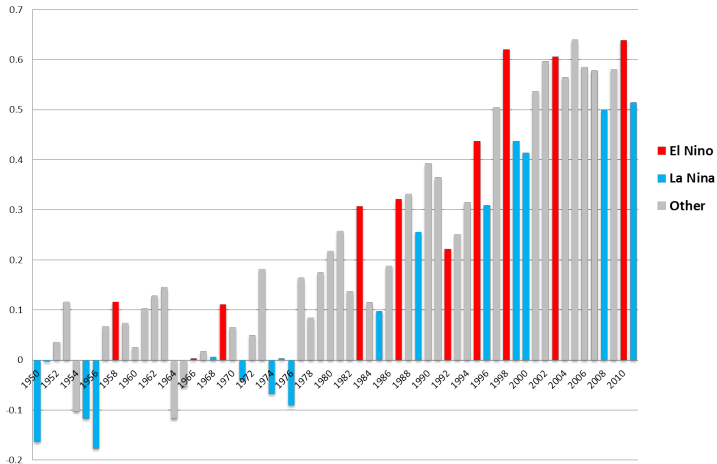


The Azimuth Project

John Baez, Jan Galkowski, Graham Jones, Nadja Kutz, Daniel Mahler, Blake Pollard, Paul Pukite, Dara Shayda, David Tanzer, David Tweed, Steve Wenner *et al*

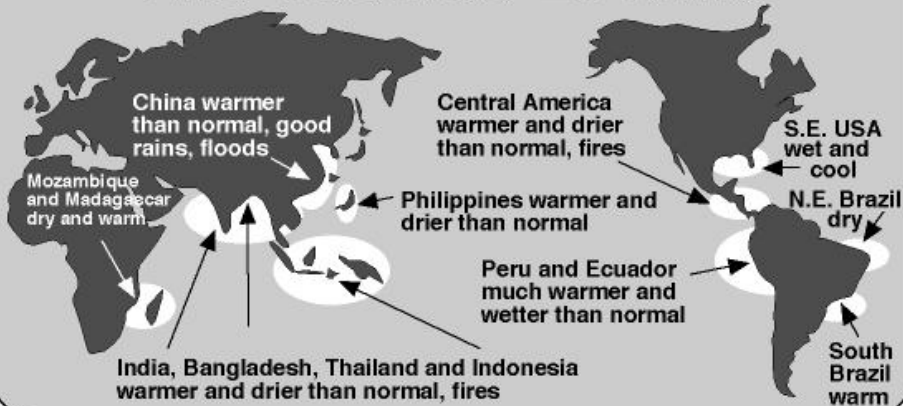
El Niño Southern Oscillation: a major source of temperature variability

Annual Global Temperature Anomalies
1950 - 2011



What is El Niño?

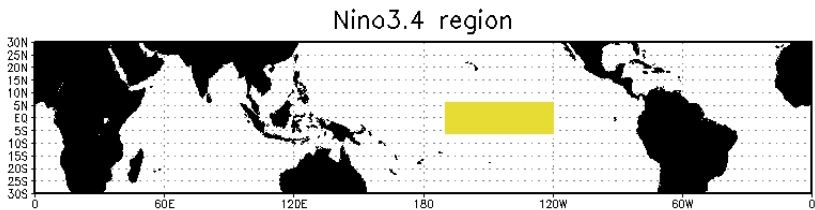
The 1997/98 El Niño



Shrimp News International

Two closely correlated signs of El Niño:

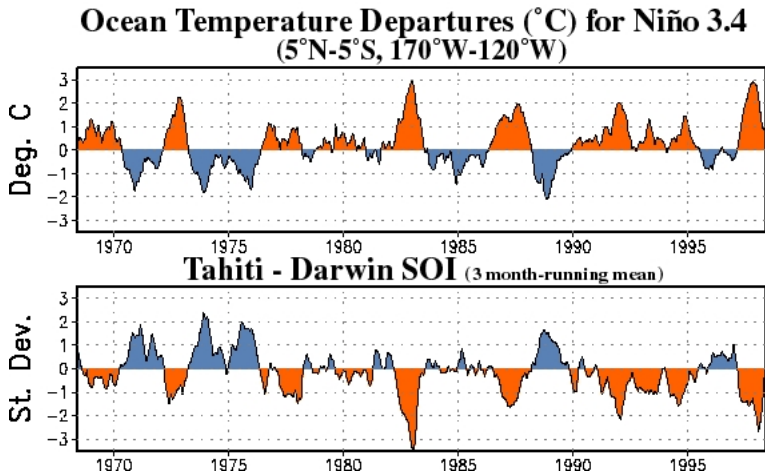
1) Increased sea surface temperatures in this region:



The **temperature anomaly** in this region—how much warmer it is than usual for this time of year—is called the **Niño 3.4 index**.

2) A decrease in air pressures in the *western* side of the Pacific compared to those further *east*. This is measured by the **Southern Oscillation Index** or **SOI**.

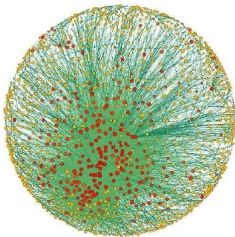
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The El Niño Southern Oscillation or **ENSO** is one of many **teleconnections**: strong correlations between weather at distant locations. These can be found using principal component analysis. ENSO is the biggest on time scales between a year and a decade.

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A new line of research is studying teleconnections using **complex network theory**: the study of large graphs found in nature and society.



Vitali, Glattfelder and Battiston:
The network of global corporate control

In complex network theory, people often start with a **weighted graph**:

- ▶ a set N of **nodes**
- ▶ for any pair of nodes $i, j \in N$, a **weight** $A_{ij} \in [0, \infty)$.

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In complex network theory, people try to compute quantities that reveal interesting information about large weighted graphs.

For example, the **in-degree** of a node $j \in N$ in a weighted graph is

$$\sum_{i \in N} A_{ij}$$

If lots of people have web pages with lots of links to yours, your webpage will have a high in-degree.

If lots of people like you on Facebook, *you* will have a high in-degree.

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Let $T_i(t)$ be the temperature anomaly at the i th grid point at month t . They compute the correlation of these variables for each pair of grid points i, j :

$$A_{ij} = \frac{\langle T_i T_j \rangle}{\sqrt{\langle T_i^2 \rangle \langle T_j^2 \rangle}}$$

This has $-1 \leq A_{ij} = A_{ji} \leq 1$.

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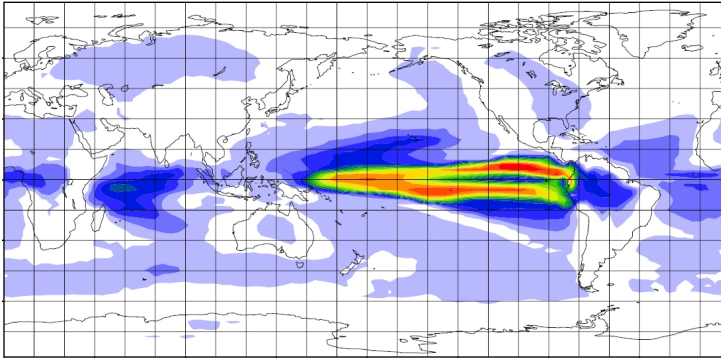
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They create a graph where there is an edge between i and j when $|A_{ij}| > c$. They adjust c so that 0.5% of the pairs i, j have an edge between them.

Then Donges *et al* plot the degree of each node, weighted by the area of its grid square:

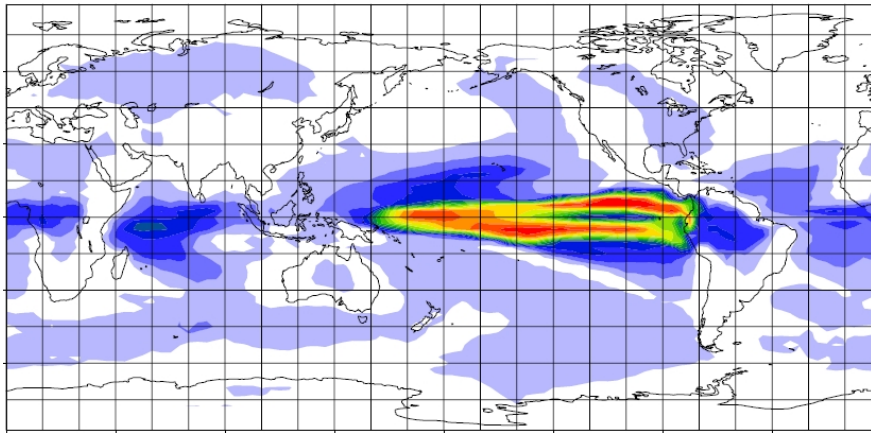


A certain patch dominates the world: the **El Niño basin**. The reddest patches are nodes connected to 5% or more of the other nodes: at least 10 times as many as average.

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No! Repeating the procedure with mutual information, Donges *et al* get this:



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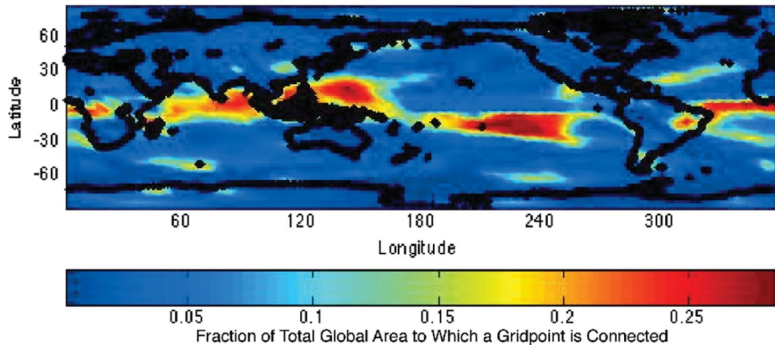
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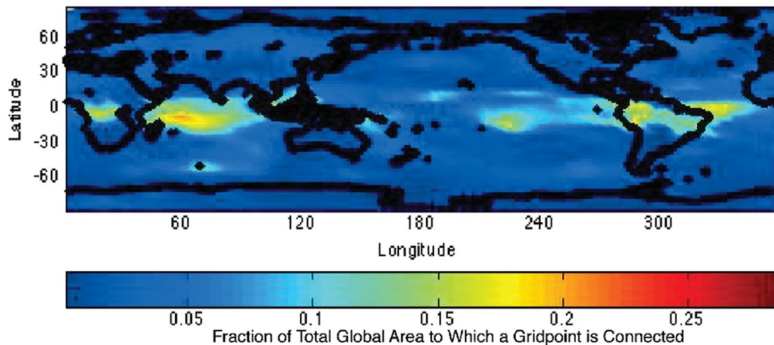
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- ▶ create a link between grid points when their correlation has absolute value greater than 0.5;
- ▶ only use temperature data from November to March in each year.

Tsonis and Swanson get this map for La Niña conditions:



and this map for El Niño conditions:



They conclude that “*El Niño breaks climate links*”.

Can we use climate networks to *predict* El Niños?

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People really want to predict El Niños, because they have huge effects on agriculture, especially around the Pacific ocean. But it's very hard to predict El Niños more than 6 months in advance!

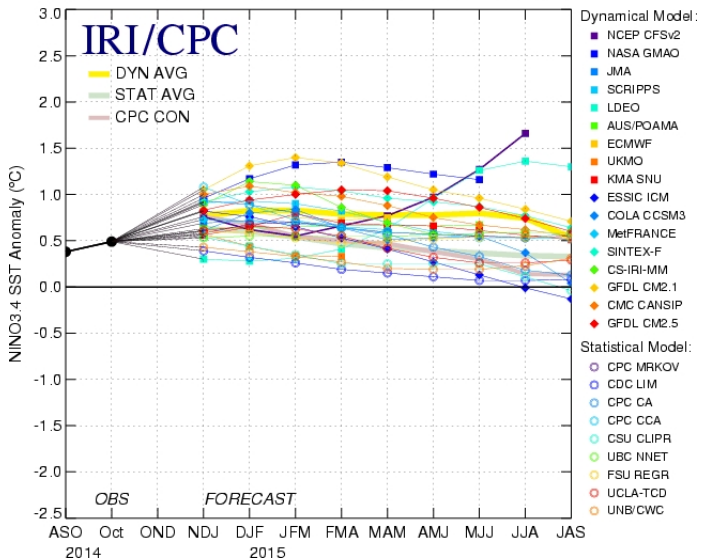
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What would we like to predict, exactly? When the 3-month running average of the Niño 3.4 index exceeds $0.5\text{ }^{\circ}\text{C}$ for 5 months, we officially declare that there is an **El Niño**.

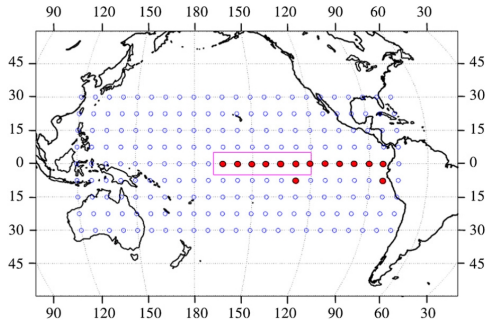
There are many teams trying to predict the Niño 3.4 index.

Mid-Nov 2014 Plume of Model ENSO Predictions



A 2013 paper by Ludescher *et al*, called *Very early warning of next El Niño*, uses a climate network for El Niño prediction.

They build their climate network using correlations between daily surface air temperature data between points *inside* the El Niño basin and certain points *outside* this region:



Ludescher *et al*

They use these correlations to construct a weighted graph. They predict an El Niño will occur if the average weight exceeds a certain threshold.

More precisely: they let $T_i(t)$ be the surface air temperature anomaly at the i grid point at time t . They consider the **time-delayed covariance** between temperatures at different grid points:

$$\langle T_i(t) T_j(t - \tau) \rangle - \langle T_i(t) \rangle \langle T_j(t - \tau) \rangle$$

where τ is a time delay and $\langle \rangle$ denotes a running average over the last year, that is:

$$\langle f(t) \rangle = \frac{1}{365} \sum_{d=0}^{364} f(t - d)$$

where t is the time in days.

They normalize this to define a correlation $C_{i,j}^t(\tau)$ that ranges from -1 to 1.

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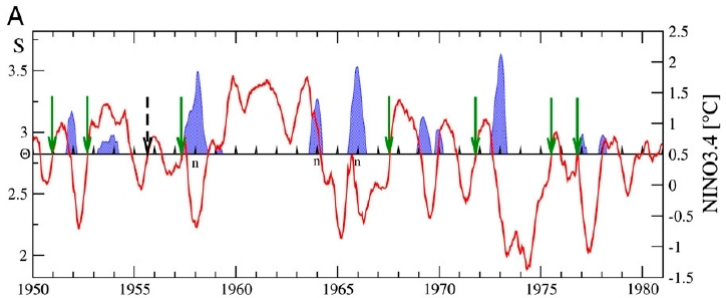
They define the **link strength** $S_{i,j}(t)$ as the difference between the maximum and the mean value of $|C_{i,j}^t(\tau)|$, divided by its standard deviation.

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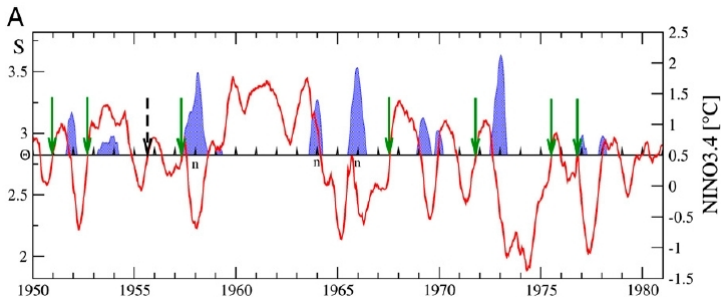
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Finally, they let $S(t)$ be the **average link strength**, calculated by averaging $S_{ij}(t)$ over all pairs i, j where i is a grid point *inside* their El Niño basin and j is a grid point *outside* this basin but still in their larger rectangle.



The blue peaks are episodes when the Niño 3.4 index exceeds 0.5 °C.



The blue peaks are episodes when the Niño 3.4 index exceeds $0.5\text{ }^{\circ}\text{C}$.

The red line is their 'average link strength'. Whenever this exceeds a certain threshold, and the Niño 3.4 index is not *already* over $0.5\text{ }^{\circ}\text{C}$, they predict it will exceed $0.5\text{ }^{\circ}\text{C}$ in the following calendar year.

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The [latest data](#) says: yes, this happened in November!

Analysis

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Their method has an 61% expected posterior probability of successfully predicting an El Niño initiation when one actually occurs — but the 95% confidence interval is huge: 39% to 80%.

How much does average link strength say about whether an El Niño is coming?

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There's a problem with small sample size. Ludescher *et al* only make a single yes-or-no prediction each year for 65 years.

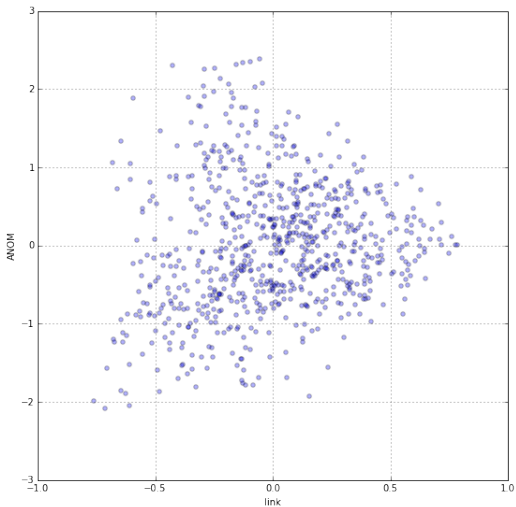
31 years were used for training their algorithm, leaving just 34 retrodictions and one actual prediction.

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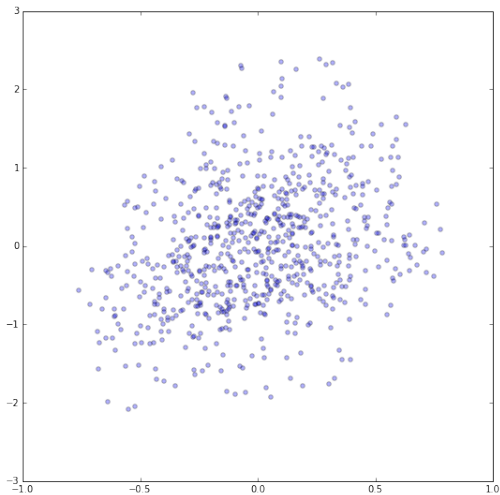
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We need more ideas! Daniel Mahler and Dara Shayda of the Azimuth Project compared simple linear regression models to more complex models and found some interesting results.



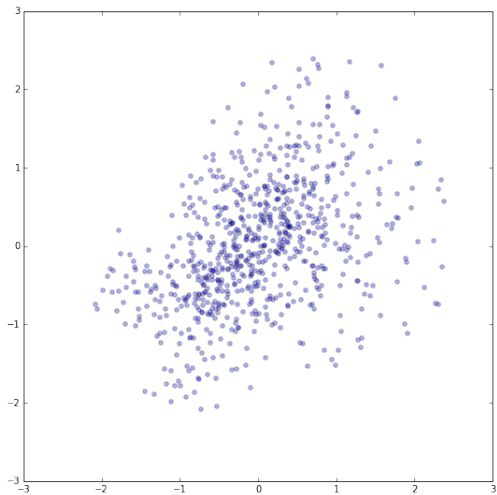
Niño 3.4 as a function of average link strength — no time lag

$$R^2 = 0.0175$$



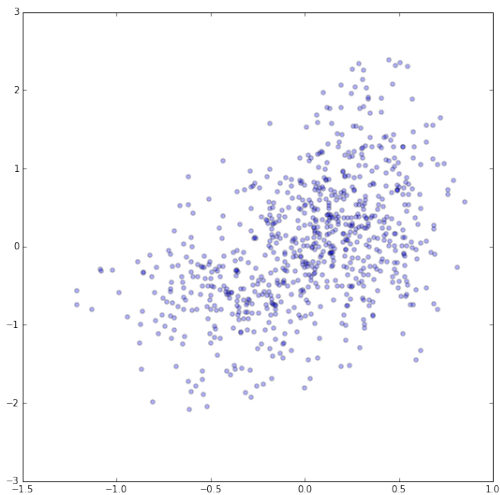
Niño 3.4 as a function of average link strength 6 months earlier

$$R^2 = 0.088$$



Niño 3.4 as a function of Niño 3.4 six months earlier

$$R^2 = 0.162$$



Niño 3.4 as a function of
average link strength and Niño 3.4 six months earlier

$$R^2 = 0.22$$

Summary

Using a linear model, the average link strength on a given month accounts for 8% of the variance of Niño 3.4 index 6 months in the future.

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The Niño 3.4 index explains 16% of its own variance 6 months into the future.

Taken together, they explain 22%. So, these two variables contain a fair amount of *independent* information about the Niño 3.4 index 6 months in the future.

Furthermore, they explain a surprisingly large amount of its variance for just 2 variables.

For comparison, Mahler used `ExtraTreesRegressor` to predict Niño 3.4 six months into the future from much larger datasets. Out of the 778 months available he trained the algorithm on the first 400 and tested it on 378.

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The result: using a `full world-wide grid of surface air temperature values` at a given moment in time explains only 23% of the Niño 3.4 six months into the future: $R^2 = 0.23$.

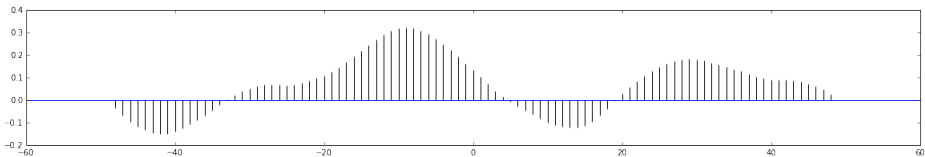
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A [full grid of surface air pressure values](#) explains 34% of the variance. Using [twelve months](#) of the full grid of pressure values only gets around 37%.

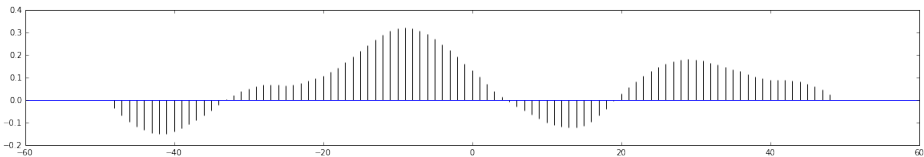
So, explaining 22% of the variance with just two variables doesn't look so bad!

Moreover, the average link strength is maximally correlated with Niño 3.4 *10 months into the future*:



(The lines here occur at monthly intervals.)

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So, *something like average link strength has predictive power for El Niños. But what is it, **exactly** — and why?*