

LAST NAME:

FIRST NAME:

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**MATH 65B - Spring 2018**

Groupwork 1: January 16, 2018

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1. Use the Fundamental Theorem of Calculus to compute the following derivative.

$$\frac{d}{dx} \int_1^{\sin(x)} \cos(t) e^{-t^3} dt$$

2. Compute the following indefinite integral.

$$\int \sin(x) \sec^2(\cos(x)) dx$$

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**Please, show all work.**

3. Compute the following definite integral.

$$\int_0^4 \frac{x}{\sqrt{1+2x}} dx$$

4. Compute the following limits.

(a)  $\lim_{x \rightarrow 0} \frac{x}{\cos(x)}$

(b)  $\lim_{x \rightarrow 1} \frac{\ln(x)}{\sin(\pi x)}$

(c)  $\lim_{x \rightarrow 0^+} x^{x^2}$

(d)  $\lim_{x \rightarrow \infty} x \tan\left(\frac{1}{x}\right)$

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Please, show all work.

5. Compute the following indefinite integral.

$$\int \frac{e^x}{1 + e^{2x}} dx$$

6. Solve the following initial value problem.

$$\frac{dy}{dx} = 1 + y^2, \quad y(0) = 0$$

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Please, show all work.