

Name: _____

Score: _____ / 100

Student ID: _____

DO NOT OPEN THE EXAM UNTIL YOU ARE TOLD TO DO SO

	1	2	3	4	5	6	7	8	9	Total
✓										70
Score										
Pts. Possible	10	5	10	5	10	10	10	10	5	75

INSTRUCTIONS FOR STUDENTS

- Questions are on both sides of the paper. This is an 9 question exam.
- Students have 1 hour and 50 minutes to complete the exam.
- The test will be out of **70 points**. The highest possible score will be **75 points**. You can attempt as many of the questions as you wish, but keep in mind you are trying to get to the **70 points**.
- In the above table, the row with the ✓, is for you to keep track of the problems you are attempting/completing.
- Higher point problems are harder, thus they are weighted more. In order to do well, you will have to attempt some of the more difficult problems.
- You may complete parts of problems, as partial credit will be given based on correctness, completeness, and ideas that are leading to the correct solutions.
- **PLEASE SHOW ALL WORK**. Any unjustified claims will receive no credit. Clearly box your final answer.
- No notes, textbooks, phones, calculators, etc. are allowed for the exam.
- The back of the test can be used for scratch work.

GOOD LUCK!

FORMULAS:

Useful Formulas	Useful Formulas
$\frac{d}{dx} \arcsin(x) = \frac{1}{\sqrt{1-x^2}} \quad x < 1$	$\int \frac{dx}{\sqrt{a^2-x^2}} = \arcsin\left(\frac{x}{a}\right) + C$
$\frac{d}{dx} \arccos(x) = -\frac{1}{\sqrt{1-x^2}} \quad x < 1$	$\int \frac{dx}{a^2+x^2} = \frac{1}{a} \arctan\left(\frac{x}{a}\right) + C$
$\frac{d}{dx} \arctan(x) = \frac{1}{1+x^2}$	$\int \frac{dx}{x\sqrt{a^2-x^2}} = \frac{1}{a} \operatorname{arcsec}\left \frac{x}{a}\right + C$
$\sin(2\theta) = 2 \sin(\theta) \cos(\theta)$	$\cos^2(\theta) = \frac{1}{2}(1 + \cos(2\theta))$
$\sin^2(x) + \cos^2(x) = 1$	$\sin^2(\theta) = \frac{1}{2}(1 - \cos(2\theta))$

- 1) (10 pts.) Compute the following indefinite integral.

$$\int x^2 \sin(2x) dx$$

2) (5 pts.) Compute the following indefinite integral.

$$\int \sin^2(x) \cos^4(x) dx$$

3) (10 pts.) Compute the following indefinite integral.

$$\int \frac{\sqrt{1+x^2}}{x} dx$$

4) (5 pts.) Compute the following indefinite integral.

$$\int \frac{5x^2 + 3x - 2}{x^3 + 2x^2} dx$$

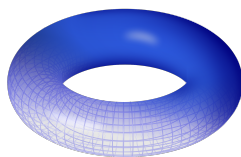
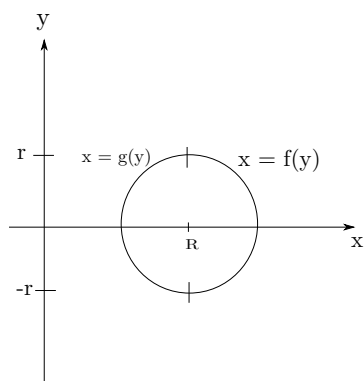
5) (10 pts.) Determine whether the integral is convergent or divergent.

$$\int_{-1}^0 \frac{e^{1/x}}{x^3} dx$$

6) (10 pts.) Find the volume of the region rotated around the x -axis, and bounded by $x = 1 + y^2$, $x = 0$, $y = 1$, and $y = 2$.

7) (10 pts.) The following question is designed to walk you through how to find the volume of the torus, the doughnut shaped solid pictured at the bottom of the page.

- a) (1 pts.) Write the equation of a circle with center at $(R, 0)$ and radius r .
- b) (2 pts.) Solve the equation of the circle you found in part (a) for x . Now, using the result, write out the functions $g(y)$ and $f(y)$ that are given in the diagram below.
- c) (4 pts.) Integrating with respect to y , set up the integral for the volume, rotating around the y -axis. We are really doing washers from scratch. We are finding the area of the large outside disk and small inner disk. (**Hint:** Since we are integrating with respect to y , the formula is no longer top – bottom, but right – left.)
- d) (3 pts.) Do the integration and find the volume, using the answer from part (c). (**Hint:** What area is $\int_{-r}^r \sqrt{r^2 - y^2} dy$ in the diagram below? Doing the integral directly is possible, but it is a trig-sub.)



8) (10 pts.) Find the area of the surface generated by rotating the loop of the curve $9y^2 = x(3 - x)^2$ about the x -axis.

9) (5 pts.) A particle is moved along the x -axis by a force that measures $\frac{10}{(1+x)^2}$ pounds at a point x feet from the origin. Find the work done in moving the particle from the origin to a distance of 9 ft.

THIS PAGE IS LEFT BLANK FOR ANY SCRATCH WORK

END OF TEST