Name: $\qquad$ Score: $\qquad$ / 100

## Student ID:

$\qquad$

DO NOT OPEN THE EXAM UNTIL YOU ARE TOLD TO DO SO

|  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\checkmark$ |  |  |  |  |  |  |  |  |  |  | 27 |
| Score |  |  |  |  |  |  |  |  |  |  |  |
| Pts. Possible | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 29 |

## INSTRUCTIONS FOR STUDENTS

- Questions are on both sides of the paper. This is an 10 question exam.
- Students have 2 hours and 15 minutes to complete the exam.
- The test will be out of 27 points. The highest possible score will be 29 points. You must complete 9 problems for credit ( 3 points each, 27 points total). If you wish, you can attempt a $10^{\text {th }}$ problem for extra credit. That question will be out of 2 points, for a maximum of 29 possible points.
- In the above table, the row with the $\checkmark$ should be marked for the 9 questions you want graded. Mark EC for the extra credit problem.
- You may complete parts of problems, as partial credit will be given based on correctness, completeness, and ideas that are leading to the correct solutions.
- PLEASE SHOW ALL WORK. Any unjustified claims will receive no credit. Clearly box your final answer.
- No notes, textbooks, phones, calculators, etc. are allowed for the exam.
- The back of the test can be used for scratch work.


## GOOD LUCK!

1) Use graph transformations to sketch the following graph. USE THE GRAPH PAPER FOR YOUR FINAL ANSWER.

$$
f(x)=-(-x+1)^{3}+2
$$


2) Use polynomial or synthetic division to divide the polynomials:

$$
\frac{x^{4}-3 x^{3}+3 x^{2}-3 x+2}{x-2}
$$

3) Put the following quadratic function in vertex form. State the vertex and axis of symmetry.

$$
f(x)=2 x^{2}-20 x+48
$$

4) Identify the asymptotes and zeros of the function. Sketch the graph. USE THE GRAPH PAPER FOR YOUR FINAL ANSWER.

$$
f(x)=\frac{x^{2}+4}{x^{2}-4}
$$


5) Solve the following rational inequality, and put the answer in interval notation:

$$
\frac{5}{2-x} \leq \frac{3}{3-x}
$$

6) Find the difference quotient $\frac{f(x+h)-f(x)}{h}$ for the function $f(x)=\sqrt{x+2}$, and reduce completely.
7) Write the inverse function, $f^{-1}(x)$, for $f(x)=2 x+9$, and check that your result is the inverse.
8) Solve the following equation for $x$ : $2 e^{2 x}+5 e^{x}-12=0$
9) Graph the following function: $f(x)=-\ln (x-1)+2$. USE THE GRAPH PAPER FOR YOUR FINAL ANSWER.

10) A bacteria culture is being created and the population is governed by the equation $P(t)=P_{0} e^{k t}$, where $P_{0}$ and $k$ are constants.
a) If the initial population is 20 bacteria, and after 5 minutes there are 100 bacteria, determine $k$ in the $P(t)$ function (Advice: You can leave the $\ln$ in the final answer).
b) Find $P(10)$. What does this quantity mean?
c) Find the time, $t$ in minutes, to reach 200 bacteria (Advice: You can leave the $\ln$ in the final answer).

THIS PAGE IS LEFT BLANK FOR ANY SCRATCH WORK

