## MILANKOVITCH CYCLES AND THE EARTH'S CLIMATE



John Baez Climate Science Seminar California State University Northridge April 26, 2013

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Understanding the Earth's climate poses different challenges at different time scales.

The Earth has been cooling for at least 15 million years, with glaciers in the Northern Hemisphere for at least 5 million years. Irregular climate cycles have been getting stronger during this time, becoming full-fledged **glacial cycles** roughly 2.5 million years ago. These cycles lasted roughly 40,000 years at first, and more recently about 100,000 years.

Let's zoom out and look at the climate over longer and longer periods of time!



### Global Land-Ocean Temperature Index

NASA Goddard Institute of Space Science



Reconstruction of temperature from 73 different records — Marcott et al.

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## Holocene Temperature Variations



8 temperature reconstructions — Global Warming Art

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Recent glacial cycles — Global Warming Art

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Oxygen isotope measurements of benthic forams, Lisiecki and Raymo

The Pliocene began 5.3 million years ago; the Pleistocene 2.6 million years ago.

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Oxygen isotope measurements of benthic forams, Zachos et al.

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- Why does the Earth tend to slowly cool and then suddenly warm within each glacial cycle?

A widely accepted theory, due to Milankovitch, says that glacial cycles are controlled by the amount of sunshine hitting the Earth at about  $65^{\circ}$  north around the Summer Solstice. This summer sunshine tends to melt glaciers.

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The amount of sunshine at different latitudes in different seasons varies due to changes in three of the Earth's orbital parameters:

- 1) precession of the Earth's axis
- 2) changes in the amount of the Earth's axial tilt
- 3) changes in the eccentricity of the Earth's orbit.



Precession has a period of roughly 23,000 years. In fact there are different components to this variation, with periods of 19, 22, and 24 kiloyears.



# The Earth's obliquity or axial tilt varies with a period of 41 kiloyears.

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The eccentricity of the Earth's orbit changes in cycles with several components, with periods of 413 kiloyears (the strongest), 125 kiloyears, and 95 kiloyears.

The orbit varies from almost circular to having an eccentricity of 0.06 (vastly exaggerated at right).

Precession and changes in obliquity do not affect the yearly *total* sunshine hitting the Earth. Changes in eccentricity do affect it, but only a small amount: just 0.167%.

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However, these changes dramatically affect the amount of sunshine hitting the Earth at a *given time of year* at a *given latitude*. On the summer solstice at  $65^{\circ}$  N, averaged over the whole day, the insolation can vary between 440 and 560 watts per square meter!

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Unfortunately, comparing this summer solstice insolation at  $65^{\circ}$  N to the Earth's glacial cycles, we do *not* say **"Aha, now the glacial cycles make perfect sense!"** 





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Nonetheless, a Fourier transform of Earth's climate data shows peaks at frequencies close to those of the Milankovich cycles!

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But my student Blake Pollard decided to try it as a little warmup project, which he published on my blog. So let's look at what he found.

Pollard compared the Earth's insolation on July 1st at  $65^{\circ}$  N as computed by André Berger to the Earth's temperature as estimated using deuterium concentrations in an ice core from the Antarctic site EPICA Dome C.

Pollard compared the Earth's insolation on July 1st at 65° N as computed by André Berger to the Earth's temperature as estimated using deuterium concentrations in an ice core from the Antarctic site EPICA Dome C. Merely graphing them together, we get a mess:



Then he took a windowed Fourier transform or 'Gabor transform' of the temperature data. This shows how the dominant frequencies of the temperature variations change with time. The yellow means a strong signal at this frequency (in inverse kiloyears):



He compared this to obliquity, which has a peak at period 41 kiloyears, so frequency 0.024 kiloyears<sup>-1</sup>:



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He compared it to eccentricity, which has peaks at periods of 413, 125, and 95 kiloyears, so frequencies of 0.0024, 0.008, and 0.011 kiloyears<sup>-1</sup>:



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He also compared it to precession, which has peaks at periods of 19, 22, and 24 kiloyears, so frequences of 0.052, 0.045 and 0.042 kiloyears<sup>-1</sup>:



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### He also compared it to insolation on July 1st at $65^{\circ}$ N:



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So: it looks as if in the last 800,000 years, variations in the Earth's temperature occur at periods that most closely match those of *obliquity* (41 kiloyear) and *eccentricity* ( $\sim$ 100 kiloyear) cycles.

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Variations in *insolation* are strongly affected by the more rapid *precession* cycles, with period  $\sim$ 20 kiloyears. But this high-frequency signal is not so strongly visible in the Earth's temperature variations.

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All this agrees with the conventional wisdom. But there are alternative theories...

Richard Muller and Gordan MacDonald argue that glacial cycles are correlated to the angle between the plane of the Earth's orbit and the plane perpendicular to the angular momentum of the Solar System. So Pollard looked at this too:



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So, perhaps the  ${\sim}100$  kiloyear variations in the Earth's temperature are explained by changes in the plane of the Earth's orbit, rather than changes in the eccentricity of its orbit.

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This leads us to our next point...

We want much more than cycles with similar frequencies to those of the Earth's temperature variations!

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We want a *physically convincing model* that will *retrodict the Earth's climate given its orbital parameters and other data.* 

In a 1998 letter in *Nature*, Didier Paillard proposed two models. I'll only present the simpler, qualitative model.

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In this simple model, the Earth can be in three different states:

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- i: interglacial
- ▶ g: mild glacial
- ► G: full glacial

In this simple model, the Earth can be in three different states:

- i: interglacial
- g: mild glacial
- ► **G**: full glacial

Moreover:

- ► The Earth goes from i to g as soon as the insolation goes below some level i<sub>0</sub>.
- The Earth goes from g to G when the insolation goes below some level i<sub>2</sub>, if it has remained below i<sub>3</sub> for at least a time t<sub>g</sub>.

► The Earth goes from **G** to **i** as soon as the insolation goes above some level *i*<sub>1</sub>.

Only the transitions  $i\to g,~g\to G$  and  $G\to i$  are allowed! The reverse transitions are forbidden.

So, the only thing required to complete Paillard's model are choices of these numbers:

$$i_0 = -0.75, \qquad i_1 = i_2 = 0, \qquad i_3 = 1$$

where insolation is measured in standard deviations from its mean value, and

 $t_g = 33$  kiloyears

which is longer than a precession cycle. His model then gives these results:



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This has been a very quick introduction to a complex field — a field I'm not an expert in.

I mainly hoped to convince you that there are many interesting problems here. They may be important for understanding abrupt climate change.