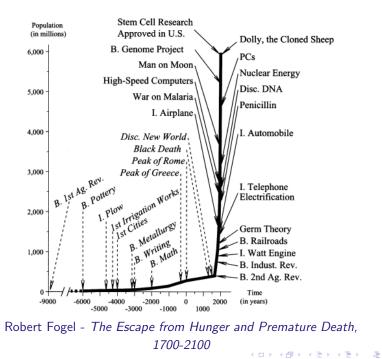
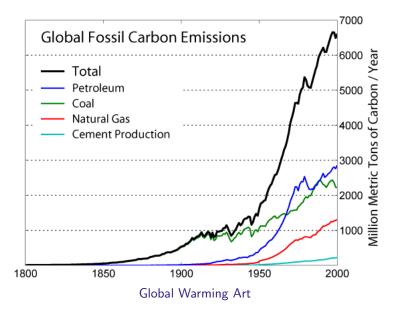
THE MATHEMATICS OF PLANET EARTH

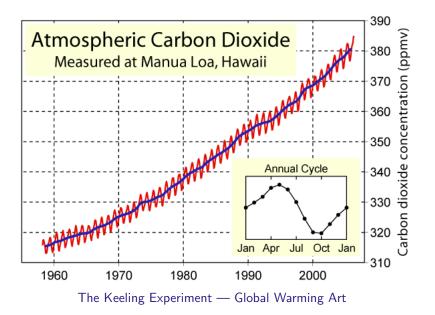
John Baez

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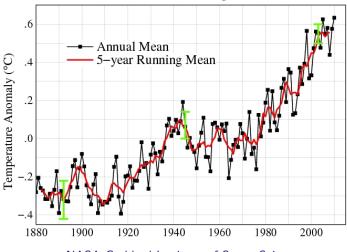




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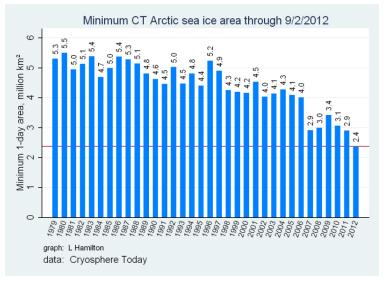


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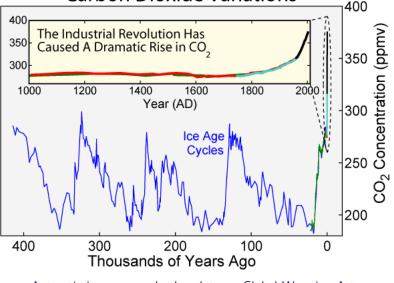
Global Land-Ocean Temperature Index

NASA Goddard Institute of Space Science



The Cryosphere Today

Carbon Dioxide Variations



Antarctic ice cores and other data — Global Warming Art

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This is when we began to systematically exploit solar power by planting crops.

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But let's go back and see how math played a role in an even bigger revolution: the Agricultural Revolution from 10,000 to 5,000 BC.

This is when we began to systematically exploit solar power by planting crops.

By now we use about 25% of all plant biomass grown worldwide! If this reaches 100% there will be, in some sense, no 'nature' separate from humanity.

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Starting shortly after the end of the last ice age, the agricultural revolution led to:

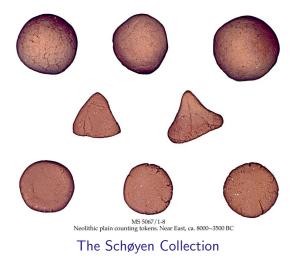
- surplus grain production, and thus kingdoms and slavery.
- astronomical mathematics for social control and crop planning.
- geometry for measuring fields and storage containers.

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written numbers for commerce.

Consider the last...

Starting around 8,000 BC, in the Near East, people started using 'tokens' for contracts: little geometric clay figures that represented things like sheep, jars of oil, and amounts of grain.



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Eventually they gave up on the tokens. The marks on tablets then developed into the Babylonian number system! The transformation was complete by 3,000 BC.

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J. J. O'Connor and E. F. Robertson, Babylonian Numerals

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It may seem like child's play now, but this 5,000-year process of abstraction—*the invention of a general notation for numbers*—laid the foundations for the math we know.

By 1700 BC the Babylonians could compute $\sqrt{2}$ to 6 decimals:

$$1 + \frac{24}{60} + \frac{51}{60^2} + \frac{10}{60^3} \approx 1.414213..$$



Yale Babylonian Collection, YBC7289

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So: what kind of mathematics will we create when we realize the planet is finite, and no longer think of ourselves as separate from nature?

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Let's optimistically assume civilization survives.

So: what kind of mathematics will we create when we realize the planet is finite, and no longer think of ourselves as separate from nature?

Let's optimistically assume civilization survives.

Math may undergo a transformation just as big as it did in the Agricultural Revolution.

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It should turn carbon dioxide into material that is buried somehow.

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But this takes energy! Making this with fossil fuels would defeat the whole purpose, so let's say the machine is solar powered.

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Even better, these machines should spread without human intervention.



If we could 'tweak' trees to sequester more CO_2 , or simply stop cutting down so many, it would make a big difference for global warming.

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This is a simple example of **ecotechnology**: technology that works *like* nature and works *with* nature.

For sophisticated ecotechnology we need to pay attention to what's already known—permaculture, systems ecology and so on. But better mathematics could help.

To understand ecosystems, ultimately will be to understand networks. - B. C. Patten and M. Witkamp

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Cao and Caldeira argue that if we double CO_2 in the air, 16% of land warming will be caused by this effect!

But CO₂ also helps plants grow leaves. Bounoua *et al* say this effect would cool the land by 0.6 $^{\circ}$ C with doubled CO₂.

What's really going on? We need biologists to go out and study leaves... but we *also* need mathematicians to think about leaves.

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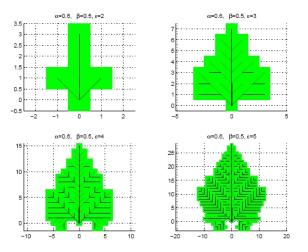
Is there math in a leaf?



Yes! A mathematician at U.C. Davis, Qinglan Xia, has written a paper called *The Formation of a Tree Leaf*.

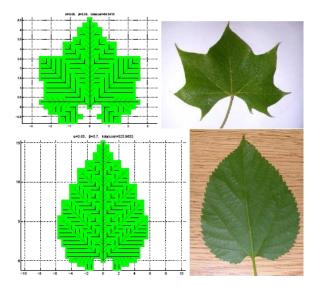
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He models a leaf as a union of square cells centered on a grid, together with 'veins' forming a weighted directed graph from the centers of the cells to the root. The leaf grows new cells at the boundary while minimizing a certain cost function.



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The cost function depends on two parameters. Changing these gives different leaf shapes:



Qinglan Xia's work is definitely math:

THE FORMATION OF A TREE LEAF

Lemma 3.8. Suppose (Ω, G) is an (ϵ, h) leaf and $(\mu, \Theta) = \phi_h(\Omega, G)$. Then the total mass of the Radon measure is bounded above by

$$\mathbf{M}(\mu) \le \pi (R_{\epsilon} + h)^2$$

and the total variation of the vector measure Θ is bounded by

$$\mathbf{M}(\Theta) \le \epsilon \pi^{2-\alpha} \left(R_{\epsilon} + h\right)^{4-2\alpha}$$
.

Proof. Since $\Omega \subset B_{R_{\epsilon}}(O)$, the mass of μ is given by

$$\begin{split} \mathbf{M}\left(\boldsymbol{\mu}\right) &= & \left|\left|\boldsymbol{\Omega}\right|\right| h^2 \\ &= & \operatorname{area}\left(\bigcup_{x\in\boldsymbol{\Omega}}\left\{x+\left[-\frac{h}{2},\frac{h}{2}\right]\times\left[-\frac{h}{2},\frac{h}{2}\right]\right\}\right) \\ &\leq & \operatorname{area}\left(B_{R_{\epsilon}+h}\left(\boldsymbol{0}\right)\right) = \pi\left(R_{\epsilon}+h\right)^2. \end{split}$$

Also, since $w(e) \leq ||\Omega|| h^2$ for each $e \in E(G)$, the total variation of Θ is given by

$$\begin{split} \mathbf{M}\left(\Theta\right) &= \sum_{e \in E(G)} w\left(e\right) length\left(e\right) \\ &\leq \left(\left|\left|\Omega\right|\right| h^{2}\right)^{1-\alpha} \sum_{m_{\beta}} m_{\beta}\left(e^{+}\right) \left(w\left(e\right)\right)^{\alpha} length\left(e\right) \end{split}$$

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This is one small part of the growing theory of networks.

This theory uses computers, because it deals with systems too complex to understand using just pencil and paper.

But it also uses much more: analysis, combinatorics, category theory, and many other branches of math.

It draws inspiration from *biology*, *ecology* and *sociology* much as the math of the industrial revolution was inspired by *physics*.

It's just beginning to be born. At the Azimuth Project we're trying to help it along.