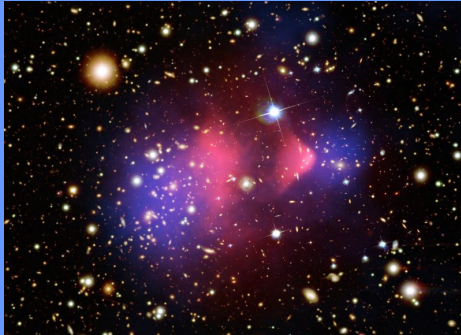


Unsolved Mysteries of Fundamental Physics



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By **fundamental physics**, I mean the search for a small set of laws which *in principle* determine everything we can calculate about the universe. The reductionist dream — not always practical, but very seductive.

Where do we stand in the search for these laws? What do we know, and what are the mysteries?

The most fundamental question:

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WHY?

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Some say that science does not tell us *why* things happen, just *what* happens. There's some truth to that.

And yet, science often moves forward by asking “why?”

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A: More than light of other colors, blue light is scattered in all directions by the Earth's atmosphere.

Q: Why is blue light scattered more?

A: Because blue light has a shorter wavelength than most other visible light.

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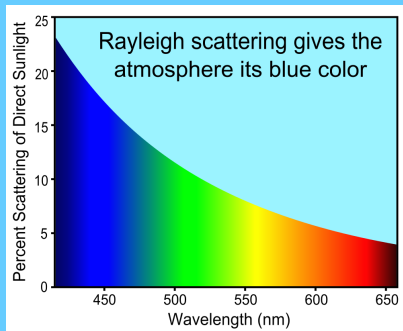
Q: So why does light with short wavelengths scatter more?

A: It scatters off oxygen and nitrogen molecules with an intensity proportional to wavelength⁻⁴.

Q: Why does light do that?

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A: Electromagnetic waves scatter off particles much smaller than their wavelength with an intensity proportional to wavelength⁻⁴.



Q: Why wavelength⁻⁴?

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A: Now that's a good question!

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A: Nobody knows.

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Q: What are the fundamental laws, if they exist?

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Q: Why is time so different from space?

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Q: Why is time so different from space?

A: Because the 'interval' between two spacetime points is

$$(\Delta s)^2 = -(\Delta t)^2 + (\Delta x)^2 + (\Delta y)^2 + (\Delta z)^2$$

in units where $c = 1$.

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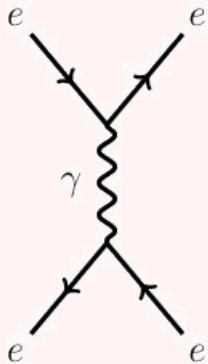
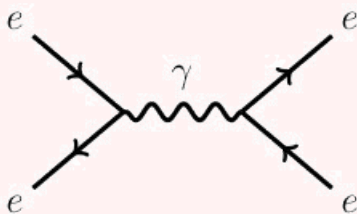
Our best theories of fundamental physics today:

STANDARD MODEL	GENERAL RELATIVITY
Electromagnetic Force Weak Force Strong Force	Gravity

The Standard Model describes all the forces *except* gravity using quantum mechanics.

General relativity describes gravity, ignoring quantum mechanics.

The Standard Model describes *particles* and their *interactions* using special relativity and quantum mechanics.



There are particles that carry forces:

electromagnetism	γ (photon)
weak force	W, Z
strong force	g (gluon)

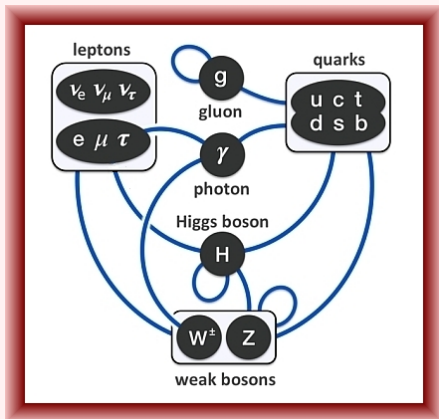
and particles that constitute 'matter':

	leptons	quarks
1st generation	e, ν_e	d, u
2nd generation	μ, ν_μ	s, c
3rd generation	τ, ν_τ	b, t

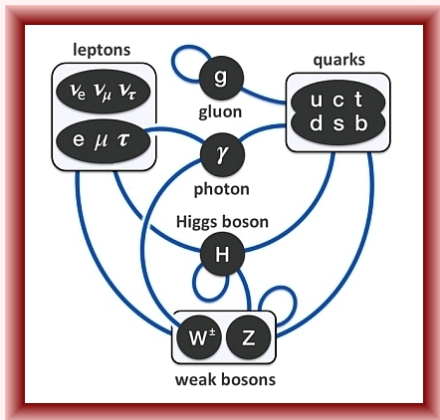
There is also one more:

H (Higgs boson)

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The strengths of their various interactions are described by 25 constants. 22 involve the Higgs boson!

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the algebra of grand unified theories

into Google.

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Q: What's up with neutrinos?

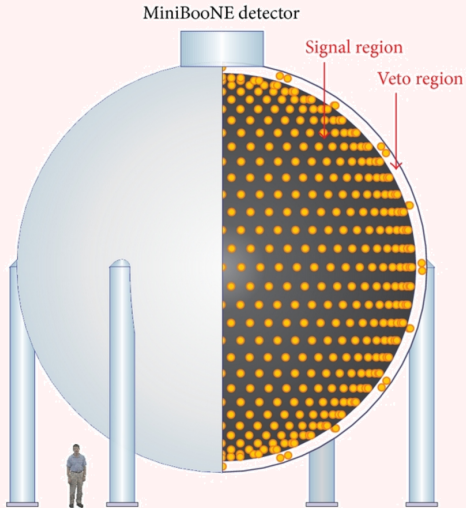
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Q: What's up with neutrinos?

Once we thought they were massless. Now we know they have masses and the 3 kinds (ν_e, ν_μ, ν_τ) can turn into each other.

In the Standard Model all this is described by their interactions with the Higgs... using 7 of the 25 constants in this model.

But there are anomalies in the data!



MiniBooNE: 800 tons of mineral oil in a tank bombarded with muon neutrinos from a distance of 500 meters... for 16 years.

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Next: MicroBooNE, with 170 tons of liquid argon!



General relativity says that freely falling objects trace out paths in spacetime that are 'as straight as possible', but that matter curves spacetime according to **Einstein's equation**:

Given any small ball of freely falling test particles initially at rest relative to each other, the rate at which its volume begins to shrink is proportional to: the energy density at the center of the ball, plus the sum of the pressures in all three directions.

or more precisely:

$$\left. \frac{\ddot{V}}{V} \right|_{t=0} = -\frac{1}{2}(\rho + P_x + P_y + P_z)$$

in units where $c = 8\pi G = 1$.

From this one can derive Newton's law of gravity in the limit of slowly moving objects and weak gravitational fields. One also can understand:

- ▶ black holes
- ▶ gravitational waves
- ▶ the Big Bang

To illustrate the simplicity of general relativity, let's *sketch* how the Big Bang works. For more details, type

the meaning of Einstein's equation

into Google!

For a long time people thought that pressure is negligible in intergalactic space except in the very early universe, giving:

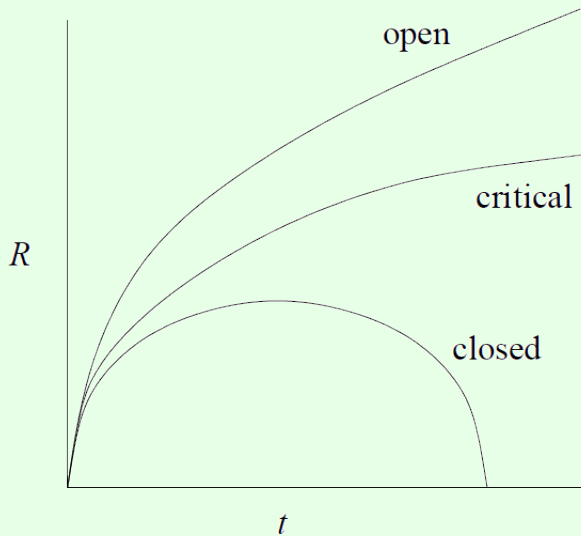
$$\frac{\ddot{V}}{V} = -\frac{\rho}{2}$$

for any ball of galaxies. Conservation of mass says ρR^3 is constant where R is the radius of the ball, so:

$$3\ddot{R} = -\frac{k}{2R^2}$$

Exactly like the motion of a rock thrown upwards from the Earth in good old Newtonian gravity! *What goes up must come down...* unless it exceeds escape velocity.

So, we get 3 possibilities:



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The most popular option is 'dark energy' with negative pressure. All we need is $6 \cdot 10^{-10}$ joules/meter³, equivalent to $7 \cdot 10^{-27}$ kilograms/meter³.

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Q: What's the ultimate fate of the Universe?

Q: Why is the future so different than the past?

Again, it seems easier to make progress on other puzzles.

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Q: Why does it seem that most of the matter in the Universe is invisible?

- ▶ Galaxies rotate faster than can be explained by all understood forms of mass.
- ▶ Our theories of galaxy formation don't work without positing 'cold dark matter'.
- ▶ Fluctuations in the microwave background radiation fit a model with cold dark matter, not a model without.

Whatever the solution to these puzzles, we are lucky that new data keeps coming in — quite quickly.

Based on the triumph of the Standard Model and general relativity by the early 1980s, theorists made the mistake of guessing that *we were close to a final theory of fundamental physics*.

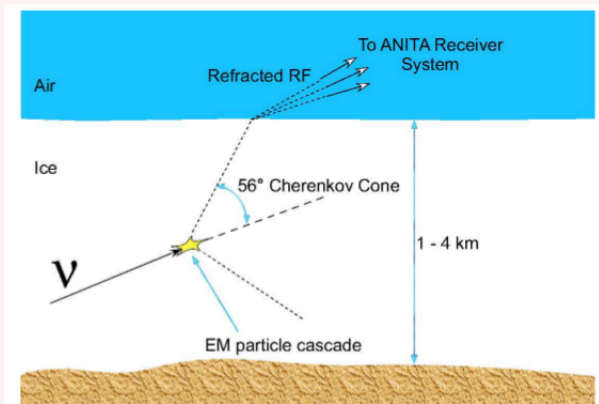
They decided to first unify the forces other than gravity, then unify them with gravity. Many hoped that *mathematical aesthetics based on existing theories could quickly finish the job*.

So far, this seems wrong.

Luckily, experiments keep revealing new clues! Last year, a paper came out with results from ANITA, the Antarctic Impulse Transient Antenna.



They seem to have seen two ultra-high-energy neutrinos — energies of $6 \cdot 10^{17}$ electron volts — *coming up through the ice*.



This seems unlikely if the Standard Model is all there is. Stay tuned!