

Local results on tangency and transversality

CHANGES TO §1.3 Some reasoning is needed to justify the condition $g^*\omega = \pm\omega$. Here is what we need:

$f: M \rightarrow M$

The natural notion of structure preserving diffeomorphism, for a contact structure, codimension 1 foliation, or indeed any hyperplane field on a manifold, is that the tangent space map of the diffeomorphism sends the hyperplane H_x at $x \in M$ to the hyperplane $H_{f(x)}$ at $f(x)$. If the hyperplane field is defined by a smooth 1-form ω (which is true for contact structures and locally for foliations near a point fixed by f^*), then

* if f is
hyperperiodic
of finite
order

the structure preserving condition is equivalent to $f^*\omega = h \cdot \omega$ where $h: M \rightarrow \mathbb{R}$ is smooth and never zero. Assume M is connected, so that h is either always positive or negative.

** Note $\omega + h \cdot \omega$ define the same hyperplane field.

PROPOSITION. Suppose f is hyperperiodic G is a finite group acting smoothly on M and \mathcal{H} is a smooth hyperplane field on M which is G -invariant.