

Mathematics 138A

Introduction to Differential Geometry — I

Course Notes

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Department of Mathematics

University of California, Riverside

Table of Contents

I.	Classical differential geometry of curves	1
1.	Cross products	2
2.	Parametrized curves	6
3.	Arc length and reparametrization	11
4.	Curvature and torsion	14
5.	Frenet-Serret Formulas	27
II.	Closed curves as boundaries	32
1.	Regions, limits and continuity	34
2.	Smooth mappings	—
3.	Inverse and implicit function theorems	—
4.	Global properties of plane curves	—
III.	Surfaces in 3-dimensional space	37
1.	Mathematica descriptions of surfaces	—
2.	Parametrizations of surfaces	—
3.	Tangent planes	—
4.	The First Fundamental Form	—
5.	Surface area	—
6.	Curves as surface intersections	—
IV.	Oriented surfaces	—
1.	Normal directions and Gauss maps	—
2.	The Second Fundamental Form	—
3.	Quadratic forms and adjoint transformations	—
4.	Normal, Gaussian and mean curvature	—
5.	Special classes of surfaces	—
6.	Compatibility equations, <i>Theorema Egregium</i>	—
7.	Fundamental Theorem of Local surface theory	—