

1. (1 pt) Library/UCSB/Stewart5.8.3/Stewart5.8.3.23.pg

Find the exact coordinates of the centroid for the region bounded by the curves $y = 4 - x^2$ and $y = 0$.

$\bar{x} = \underline{\hspace{2cm}}$

$\bar{y} = \underline{\hspace{2cm}}$

Correct Answers:

- 0
- 8/5

2. (1 pt) Library/UCSB/Stewart5.8.3/Stewart5.8.3.24.pg

Find the exact coordinates of the centroid for the region bounded by the curves $3x + 2y = 6$, $y = 0$, and $x = 0$.

$\bar{x} = \underline{\hspace{2cm}}$

$\bar{y} = \underline{\hspace{2cm}}$

Correct Answers:

- 2/3
- 1

3. (1 pt) Library/UCSB/Stewart5.8.3/Stewart5.8.3.25.pg

Find the exact coordinates of the centroid for the region bounded by the curves $y = e^x$, $y = 0$, $x = 0$, and $x = 1$.

$\bar{x} = \underline{\hspace{2cm}}$

$\bar{y} = \underline{\hspace{2cm}}$

Correct Answers:

- $1 / (\exp(1) - 1)$
- $(\exp(1) + 1) / 4$

4. (1 pt) Library/UCSB/Stewart5.8.3/Stewart5.8.3.26.pg

Find the exact coordinates of the centroid for the region bounded by the curves $y = 1/x$, $y = 0$, $x = 1$, and $x = 2$.

$\bar{x} = \underline{\hspace{2cm}}$

$\bar{y} = \underline{\hspace{2cm}}$

Correct Answers:

- $1 / \ln(2)$
- $1 / (4 * \ln(2))$

5. (1 pt) Library/UCSB/Stewart5.8.3/Stewart5.8.3.27.pg

Find the exact coordinates of the centroid for the region bounded by the curves $y = \sqrt{x}$ and $y = x$.

$\bar{x} = \underline{\hspace{2cm}}$

$\bar{y} = \underline{\hspace{2cm}}$

Correct Answers:

- 2/5
- 1/2

6. (1 pt) Library/UCSB/Stewart5.8.3/Stewart5.8.3.28.pg

Find the exact coordinates of the centroid for the region bounded by the curves $y = x + 2$ and $y = x^2$.

$\bar{x} = \underline{\hspace{2cm}}$

$\bar{y} = \underline{\hspace{2cm}}$

Correct Answers:

- 1/2
- 8/5

7. (1 pt) Library/UCSB/Stewart5.8.3/Stewart5.8.3.29.pg

Find the exact coordinates of the centroid for the region bounded by the curves $y = \sin(x)$, $y = \cos(x)$, $x = 0$, and $x = \pi/4$.

$\bar{x} = \underline{\hspace{2cm}}$

$\bar{y} = \underline{\hspace{2cm}}$

Correct Answers:

- $(\pi * \sqrt{2} - 4) / (4 * (\sqrt{2} - 1))$
- $1 / (4 * (\sqrt{2} - 1))$

1. (1 pt) Library/UCSB/Stewart5.7.8/Stewart5.7.8.6.pg

Consider the integral

$$\int_{-\infty}^0 \frac{-3}{2x-5} dx$$

If the integral is divergent, type an upper-case "D". Otherwise, evaluate the integral.

Correct Answers:

- D

2. (1 pt) Library/UCSB/Stewart5.7.8/Stewart5.7.8.8.pg

Consider the integral

$$\int_0^{\infty} \frac{3x}{(x^2+2)^2} dx$$

If the integral is divergent, type an upper-case "D". Otherwise, evaluate the integral.

Correct Answers:

- 3/4

3. (1 pt) Library/UCSB/Stewart5.7.8/Stewart5.7.8.10.pg

Consider the integral

$$\int_{-\infty}^{-1} 1e^{-2t} dt$$

If the integral is divergent, type an upper-case "D". Otherwise, evaluate the integral.

Correct Answers:

- D

4. (1 pt) Library/UCSB/Stewart5.7.8/Stewart5.7.8.12.pg

Consider the integral

$$\int_{-\infty}^{\infty} (-3 - v^4) dv$$

If the integral is divergent, type an upper-case "D". Otherwise, evaluate the integral.

Correct Answers:

- D

5. (1 pt) Library/UCSB/Stewart5.7.8/Stewart5.7.8.18.pg

Consider the integral

$$\int_0^{\infty} \frac{-10}{z^2 + 3z + 2} dz$$

If the integral is divergent, type an upper-case "D". Otherwise, evaluate the integral.

Correct Answers:

- $-10 \ln(2)$

6. (1 pt) Library/UCSB/Stewart5.7.8/Stewart5.7.8.20.pg

Consider the integral

$$\int_{-\infty}^6 -5re^{r/3} dr$$

If the integral is divergent, type an upper-case "D". Otherwise, evaluate the integral.

Correct Answers:

- $9 \cdot 5 \cdot \exp(2)$

7. (1 pt) Library/UCSB/Stewart5.7.8/Stewart5.7.8.28.pg

Consider the integral

$$\int_0^3 \frac{-10}{x\sqrt{x}} dx$$

If the integral is divergent, type an upper-case "D". Otherwise, evaluate the integral.

Correct Answers:

- D

8. (1 pt) Library/UCSB/Stewart5.7.8/Stewart5.7.8.32.pg

Consider the integral

$$\int_0^1 \frac{-1}{\sqrt{1-x^2}} dx$$

If the integral is divergent, type an upper-case "D". Otherwise, evaluate the integral.

Correct Answers:

- $-1 \cdot \pi / 2$

9. (1 pt) Library/UCSB/Stewart5.7.8/Stewart5.7.8.40.pg

Consider the integral

$$\int_0^1 \frac{-2 \ln(x)}{\sqrt{x}} dx$$

If the integral is divergent, type an upper-case "D". Otherwise, evaluate the integral.

Correct Answers:

- $-2 \cdot -4$

1. (1 pt) Library/UCSB/Stewart5.8.1/Stewart5.8.1.1.pg

Use the arc length formula to find the length of the curve

$$y = 2 - 3x, \quad -2 \leq x \leq 1.$$

You can check your answer by noting the shape of the curve.

Arc length = _____

Correct Answers:

- $3\sqrt{10}$

2. (1 pt) Library/UCSB/Stewart5.8.1/Stewart5.8.1.3.pg

Find the exact length of the curve

$$y = \frac{2}{3}(x^2 - 1)^{3/2}, \quad 1 \leq x \leq 3.$$

Arc length = _____

Correct Answers:

- $46/3$

3. (1 pt) Library/UCSB/Stewart5.8.1/Stewart5.8.1.4.pg

Find the exact length of the curve

$$y = \frac{x^3}{6} + \frac{1}{2x}, \quad \frac{1}{2} \leq x \leq 1.$$

Arc length = _____

Correct Answers:

- $31/48$

4. (1 pt) Library/UCSB/Stewart5.8.1/Stewart5.8.1.5.pg

Find the length of the curve

$$y = 1 + 6x^{3/2}, \quad 0 \leq x \leq 1.$$

Arc length = _____

Correct Answers:

- $164/243 \cdot 82^{1/2} - 2/243$

5. (1 pt) Library/UCSB/Stewart5.8.1/Stewart5.8.1.8.pg

Find the length of the curve

$$y = \frac{x^2}{2} - \frac{\ln(x)}{4}, \quad 2 \leq x \leq 4.$$

Arc length = _____

Correct Answers:

- $6 + \ln(2) / 4$

6. (1 pt) Library/UCSB/Stewart5.8.1/Stewart5.8.1.10.pg

Find the length of the curve

$$y = \ln(\cos(x)), \quad 0 \leq x \leq \pi/3.$$

Arc length = _____

Correct Answers:

- $\ln(2+3^{1/2})$

7. (1 pt) Library/UCSB/Stewart5.8.1/Stewart5.8.1.12.pg

Find the length of the curve

$$y = \ln(x), \quad 1 \leq x \leq \sqrt{3}.$$

Arc length = _____

Correct Answers:

- $2 - \sqrt{2} + \ln(\sqrt{2} + 1) - 1/2 \ln(3)$

8. (1 pt) Library/UCSB/Stewart5.8.1/Stewart5.8.1.13.pg

Find the length of the curve

$$y = \cosh(x), \quad 0 \leq x \leq 1.$$

Arc length = _____

Correct Answers:

- $1/2(\exp(1) - 1/\exp(1))$

9. (1 pt) Library/UCSB/Stewart5.8.1/Stewart5.8.1.15.pg

Find the length of the curve

$$y = e^x, \quad 0 \leq x \leq 1.$$

Arc length = _____

Correct Answers:

- $\sqrt{1 + \exp(2)} - \sqrt{2} + \ln(\sqrt{1 + \exp(2)} - 1) - 1 - \ln(\sqrt{2} - 1)$

10. (1 pt) Library/UCSB/Stewart5.8.1/Stewart5.8.1.17.pg

Which of the following integrals represents the length of the curve $y = \cos(x)$, $0 \leq x \leq 2\pi$?

- A. $\int_0^{2\pi} \sqrt{1 + \cos^2(x)} dx$
- B. $\int_0^{2\pi} \sqrt{1 + \sin^2(x)} dx$
- C. $\int_0^{2\pi} \sqrt{1 - \sin^2(x)} dx$
- D. $\int_0^{2\pi} \sqrt{1 + \sin(x)} dx$
- E. $\int_0^{2\pi} \sqrt{1 + \cos(x)} dx$
- F. $\int_0^{2\pi} \sqrt{1 + \cos^2(x)} dx$

Correct Answers:

- B

11. (1 pt) Library/UCSB/Stewart5.8.1/Stewart5.8.1.18.pg

Which of the following integrals represents the length of the curve $y = 2^x$, $0 \leq x \leq 3$?

- A. $\int_0^3 \sqrt{1 + 2^{2x}} dx$
- B. $\int_0^3 \sqrt{1 + 2(\ln 2)^2 2^x} dx$
- C. $\int_0^3 \sqrt{1 + (\ln 2)^2 2^{2x}} dx$
- D. $\int_0^3 \sqrt{1 + 2^x} dx$
- E. $\int_0^3 \sqrt{1 + (\ln 2)^2 2^{2x}} dx$
- F. $\int_0^3 \sqrt{1 + (\ln 2)^2 2^x} dx$

Correct Answers:

- C

12. (1 pt) Library/UCSB/Stewart5.8.1/Stewart5.8.1.20.pg

Which of the following integrals represents the length of the curve $\frac{x^2}{25} + \frac{y^2}{36} = 1$?

- A. $\int_{-6}^6 \left(1 + \frac{36x^2}{25(5-x^2)}\right)^{1/2} dx$
- B. $\int_{-5}^5 \left(1 + \frac{36x^2}{25(25-x^2)}\right)^{1/2} dx$
- C. $\int_{-5}^5 \left(1 + \frac{36x^2}{25(5-x^2)}\right)^{1/2} dx$
- D. $\int_{-6}^6 \left(1 + \frac{36x^2}{6(5-x^2)}\right)^{1/2} dx$
- E. $\int_{-6}^6 \left(1 + \frac{36x^2}{25(25-x^2)}\right)^{1/2} dx$
- F. $\int_{-5}^5 \left(1 + \frac{36x^2}{6(5-x^2)}\right)^{1/2} dx$

Correct Answers:

- B

Assignment 11.5 SURFACE AREA due 12/31/2012 at 08:00am PST

1. (1 pt) Library/UCSB/Stewart5.8.2/Stewart5.8.2.1.pg

Which of the following integrals represents the area of the surface obtained by rotating the curve $y = \ln(x)$, $1 \leq x \leq 3$, about the x -axis?

- A. $2\pi \int_1^3 x\sqrt{1+(1/x)^2} dx$
- B. $2\pi \int_1^3 x\sqrt{1+(1/x)^2} dx$
- C. $2\pi \int_1^3 \ln(x)\sqrt{1-(1/x)^2} dx$
- D. $2\pi \int_1^3 x\sqrt{1+(1/x)^2} dx$
- E. $2\pi \int_1^3 \ln(x)\sqrt{1+(1/x)} dx$
- F. $2\pi \int_1^3 \ln(x)\sqrt{1+(1/x)^2} dx$

Correct Answers:

- F

2. (1 pt) Library/UCSB/Stewart5.8.2/Stewart5.8.2.2.pg

Which of the following integrals represents the area of the surface obtained by rotating the curve $y = \sin^2(x)$, $0 \leq x \leq \pi/2$, about the x -axis?

- A. $2\pi \int_0^{\pi/2} \sin^2(x)\sqrt{1+(2\sin(x)\cos(x))^2} dx$
- B. $2\pi \int_0^{\pi/2} \sin^2(x)\sqrt{1+(2\sin(x))^2} dx$
- C. $2\pi \int_0^{\pi/2} x\sqrt{1+2\sin(x)\cos(x)} dx$
- D. $2\pi \int_0^{\pi/2} x\sqrt{1+(2\sin(x)\cos(x))^2} dx$
- E. $2\pi \int_0^{\pi/2} x\sqrt{1+(\sin(x)\cos(x))^2} dx$
- F. $2\pi \int_0^{\pi/2} \sin^2(x)\sqrt{1+(\sin(x)\cos(x))^2} dx$

Correct Answers:

- A

3. (1 pt) Library/UCSB/Stewart5.8.2/Stewart5.8.2.3.pg

Which of the following integrals represents the area of the surface obtained by rotating the curve $y = \sec(x)$, $0 \leq x \leq \pi/4$, about the y -axis?

- A. $2\pi \int_0^{\pi/4} \sec(x)\sqrt{1+(\sec(x)\tan(x))^2} dx$
- B. $2\pi \int_0^{\pi/4} x\sqrt{1+(2\sec(x)\tan(x))^2} dx$

- C. $2\pi \int_0^{\pi/4} \sec(x)\sqrt{1+(\tan^2(x))^2} dx$
- D. $2\pi \int_0^{\pi/4} \sec(x)\sqrt{1+(2\sec(x)\tan(x))^2} dx$
- E. $2\pi \int_0^{\pi/4} x\sqrt{1+(\sec(x)\tan(x))^2} dx$
- F. $2\pi \int_0^{\pi/4} x\sqrt{1+(\tan^2(x))^2} dx$

Correct Answers:

- E

4. (1 pt) Library/UCSB/Stewart5.8.2/Stewart5.8.2.4.pg

Which of the following integrals represents the area of the surface obtained by rotating the curve $y = e^x$, $1 \leq y \leq 2$, about the y -axis?

- A. $2\pi \int_1^2 \ln(y)\sqrt{1+(1/y)} dy$
- B. $2\pi \int_1^2 e^y\sqrt{1+(1/y)} dy$
- C. $2\pi \int_1^2 e^y\sqrt{1+(1/y)^2} dy$
- D. $2\pi \int_1^2 y\sqrt{1+(1/y)} dy$
- E. $2\pi \int_1^2 y\sqrt{1+(1/y)^2} dy$
- F. $2\pi \int_1^2 \ln(y)\sqrt{1+(1/y)^2} dy$

Correct Answers:

- F

5. (1 pt) Library/UCSB/Stewart5.8.2/Stewart5.8.2.6.pg

Find the area of the surface obtained by rotating the curve $9x = y^2 + 18$, $2 \leq x \leq 6$, about the x -axis.

Area = _____

Correct Answers:

- 49π

6. (1 pt) Library/UCSB/Stewart5.8.2/Stewart5.8.2.7.pg

Find the area of the surface obtained by rotating the curve $y = \sqrt{x}$, $4 \leq x \leq 9$, about the x -axis.

Area = _____

Correct Answers:

- $\pi/6 * (37\sqrt{37}) - 17\sqrt{17}$

7. (1 pt) Library/UCSB/Stewart5.8.2/Stewart5.8.2.8.pg

Find the area of the surface obtained by rotating the curve $y = \cos(2x)$, $0 \leq x \leq \pi/6$, about the x -axis.

Area = _____

Correct Answers:

- $\pi * (\sqrt{3})/2 + 1/4 * \ln(2 + \sqrt{3})$

8. (1 pt) Library/UCSB/Stewart5.8.2/Stewart5.8.2.9.pg

Find the area of the surface obtained by rotating the curve $y = \cosh(x)$, $0 \leq x \leq 1$, about the x -axis.

Area = _____

Correct Answers:

- $\pi * (1 + 1/2 * \sinh(2))$

9. (1 pt) Library/UCSB/Stewart5.8.2/Stewart5.8.2.10.pg

Find the area of the surface obtained by rotating the curve $y = \frac{x^3}{6} + \frac{1}{2x}$, $\frac{1}{2} \leq x \leq 1$, about the x -axis.

Area = _____

Correct Answers:

- $263/256 * \pi$

10. (1 pt) Library/UCSB/Stewart5.8.2/Stewart5.8.2.12.pg

Find the area of the surface obtained by rotating the curve $x = 1 + 2y^2$, $1 \leq y \leq 2$, about the x -axis.

Area = _____

Correct Answers:

- $\pi/24 * (65 * \sqrt{65}) - 17 * \sqrt{17}$

11. (1 pt) Library/UCSB/Stewart5.8.2/Stewart5.8.2.14.pg

Find the area of the surface obtained by rotating the curve $y = 1 - x^2$, $0 \leq x \leq 1$, about the y -axis.

Area = _____

Correct Answers:

- $\pi/6 * (5 * \sqrt{5}) - 1$

12. (1 pt) Library/UCSB/Stewart5.8.2/Stewart5.8.2.16.pg

Find the area of the surface obtained by rotating the curve $x = a \cosh(y/a)$, $-a \leq y \leq a$, about the y -axis.

Area = _____

Correct Answers:

- $2 * \pi * a^2 * (1 + 1/2 * \sinh(2))$