Answers to selected exercises from Colley, Section 2.8

28. We begin by finding the partial derivatives of the function u(x, y) = (x + y)/xy:

$$\frac{\partial u}{\partial x} = \frac{-y^2}{x^2 y^2}, \qquad \frac{\partial u}{\partial y} = \frac{x^2}{x^2 y^2}$$

Now w = f(u), so by the Chain Rule we have

$$x^2 w_x - y^2 w_y = x^2 u_x f' - y^2 u_y f'$$

and if we substitute the previously derived expressions for u_x and u_y we obtain something that simplifies to 0.