## Answers to selected exercises from Colley, Section 2.8

28. We begin by finding the partial derivatives of the function $u(x, y)=(x+y) / x y$ :

$$
\frac{\partial u}{\partial x}=\frac{-y^{2}}{x^{2} y^{2}}, \quad \frac{\partial u}{\partial y}=\frac{x^{2}}{x^{2} y^{2}}
$$

Now $w=f(u)$, so by the Chain Rule we have

$$
x^{2} w_{x}-y^{2} w_{y}=x^{2} u_{x} f^{\prime}-y^{2} u_{y} f^{\prime}
$$

and if we substitute the previously derived expressions for $u_{x}$ and $u_{y}$ we obtain something that simplifies to 0 .

