

Exercises for Week 02

1. Suppose that L is a line in P (plane) and $A, B, C \in P$ satisfy (i) $A \neq B$ on opposite sides of L , (ii) $B \neq C$ on opposite sides of L . Prove that $A \neq C$ on the same side of L .

2. Consider the analogous question if we replace "opposite sides" by "the same side". What conclusion, if any, can be drawn?

3. L and P as above with $L = CD$. If $A \neq B$ are on the same side of CD , are $C \neq D$ on the same side of AB ? The options are always yes, always no, or either is possible. Either prove this (options 1+2) or give examples (option 3).

4. In the definition of a triangle's interior, show $\text{Int } \triangle ABC = \text{Int } \triangle ABC \cap \text{Int } \triangle BCA$.

Postpone till after L4

5. Why is $\triangle ABC$ equilateral $\Leftrightarrow |\angle BAC| = |\angle ABC| = |\angle ACB|$?

6. Suppose $D \in \text{Int } \triangle ABC$. Prove that $\text{Int } \triangle DBC \subseteq \text{Int } \triangle ABC$.
7. Suppose that $L \subseteq P$ and $A, B \in P$ are such that $AB \cap L = \emptyset$. Prove that all points of \overline{AB} lie on the same side of L .
8. If $AB \cap CD = \emptyset$ (in plane) and $AD \cap BC = \emptyset$ why do A, B, C, D form the vertices of a convex quadrilateral?
9. Suppose D & C on same side AB but $BD \neq BC$ and $D \notin \text{Int } \triangle CBA$. Prove that $C \in \text{Int } \triangle ABD$. (Compare with material in L4)
10. Suppose $A, B, C, D \in P$, no 3 collinear with $CA \perp AB$ and $DB \perp AB$. Prove that $CA \cap BD = \emptyset$ (i.e., parallel)