TOPICS FOR MATHEMATICS 133, FALL 2007

Preface

I. Topics from linear algebra

- 1. Dot products
- 2. Cross products
- 3. Linear varieties
- 4. Barycentric coordinates
- 5. Some examples

II. Vector algebra and Euclidean geometry

- 1. Approaches to Euclidean geometry
- 2. Synthetic axioms of order and separation
- 3. Measurement axioms
- 4. Congruence, superposition and isometries
- 5. Euclidean parallelism

III. Basic Euclidean concepts and theorems

- 1. Perpendicular lines and planes
- 2. Basic theorems on triangles
- 3. Convex polygons
- 4. Concurrence theorems
- 5. Similarity
- 6. Circles and classical constructions
- 7. Areas and volumes

IV. Projective geometry [NOT COVERED IN THE COURSE]

- 1. Perspective images
- 2. Adjoining ideal points
- 3. Homogeneous coordinates
- 4. Duality
- 5. Theorems of Desargues and Pappus
- 6. Projective collineations and cross ratios

V. Introduction to hyperbolic geometry

- 1. Facts from spherical geometry
- 2. Attempts to prove Euclid's Fifth Postulate
- 3. Neutral geometry
- 4. Angle defects and related phenomena
- 5. Further topics in hyperbolic geometry
- 6. Subsequent developments
- 7. Non Euclidean geometry in modern mathematics