

SOLUTIONS TO ADDITIONAL EXERCISES FOR III.1 AND III.2

Here are the solutions to the exercises at the end of the file `polyangles.pdf`.

P1. Since the sum of the measures of all three face angles is at most 360° and the sum of two of the measures is 320° , it follows that the measure of the third is at most 40° . ■

P2. Let Q be the plane which is the perpendicular bisector of $[BC]$, so that a point is on Q if and only if it is equidistant from B and C . It will suffice to prove that V, A, M are all equidistant from B and C ; note that the three points in question cannot be collinear, for if they were then A would lie in the plane containing V, B, C .

We are given that V and M are equidistant from B and C , so we need only show that the same is true for A . Since $d(V, B) = d(V, C)$, $|\angle AVC| = |\angle AVB|$, and $d(V, B) = d(V, C)$, by **SAS** we have $\triangle AVB \cong \triangle AVC$, and this implies the desired equality $d(A, B) = d(A, C)$. ■