

# Viviani's curve

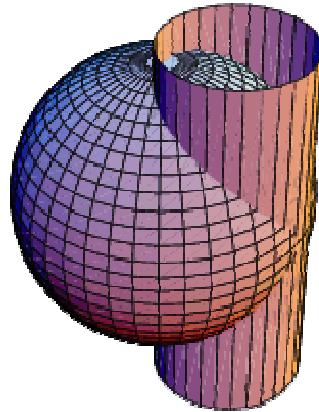
This curve is given by intersecting the unit sphere of radius  $2a$  with equation

$$x^2 + y^2 + z^2 = 4a^2$$

with the cylinder centered at  $(a, 0, 0)$  of radius  $a$  given by

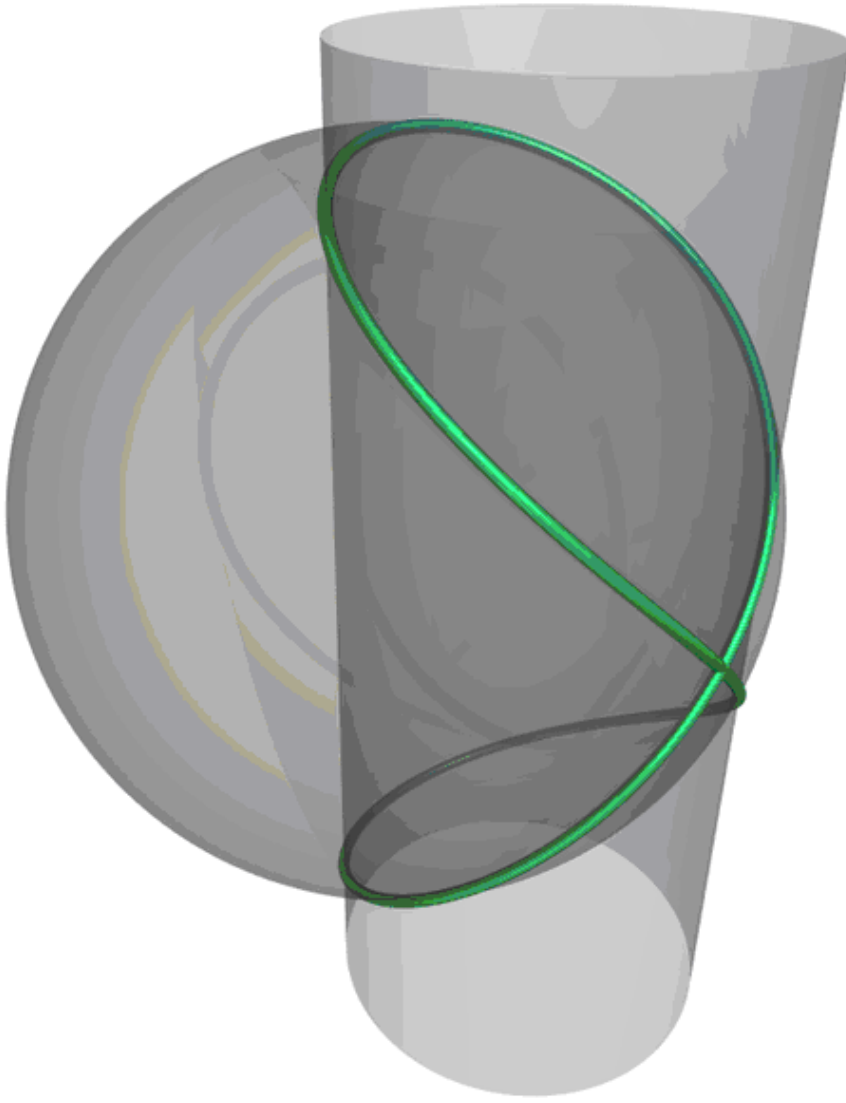
$$(x - a)^2 + y^2 = a^2.$$

For the example in the notes we have  $a = 1$ . This curve was first studied by Vincenzo Viviani (1622 – 1703).



(Source: <http://mathworld.wolfram.com/VivianisCurve.html>)

These two surfaces meet transversely everywhere except at the point  $(2a, 0, 0)$ . The curve looks like a figure eight centered at  $(2a, 0, 0)$ . An illustration appears on the next page; the parametric equations for the curve when  $a = 1$  are given in the notes.



(Source: [http://en.wikipedia.org/wiki/Sphere%E2%80%93cylinder\\_intersection](http://en.wikipedia.org/wiki/Sphere%E2%80%93cylinder_intersection))