

Recursive procedure for the method of false position

Here is an outline which can be converted into a program for finding the successive approximations to a root by the method of false position; one can even construct a program of this sort on some electronic spreadsheets. For example, a spreadsheet was used to compute the examples in <http://math.ucr.edu/~res/math153-2019/history01c.pdf>.

Starting point: We are given an interval $[LX, RX]$ and a reasonable function F which is defined on this interval. We further assume that $LY = F(LX)$ and $RY = F(RX)$ satisfy the inequality $RX < 0 < RY$. Finally, we are given a small positive number h which is needed because evaluating F on the approximations to the roots will almost never be zero, but if the absolute value of F at an approximation is within h of zero the approximate root will probably be adequate for our purposes.

TRIAL = (LX*RY – LY*RX)/(RY – LY) %% NOTE: *This is the root of the linear function whose graph passes through (LX,LY) and (RX,RY)*

IF F(TRIAL) = 0 THEN ROOT = TRIAL: END

ELSE IF F(TRIAL) < 0 THEN new LX = TRIAL, new LY = F(TRIAL)

ELSE IF F(TRIAL) > 0 THEN new RX = TRIAL, new RY = F(TRIAL)

Repeat until **ABS.VAL. F(TRIAL) < h**

When the inequality in the previous line is satisfied, the desired root of F will normally be approximately equal to **TRIAL**, and one can usually guess the degree of precision for this approximation by looking at the sequence of successive approximations obtained by the process. This is apparent in the two examples considered in the previously cited document.