## Quiz 1, Spring 2019

## Each discussion section was given one of $11-12$ or $21-22$.

11. Find the Egyptian fraction expansion for 7/26.
12. The pentagonal numbers are given by $\mathbf{P}(\mathbf{2})=5$ and $\mathbf{P}(\boldsymbol{n}+\mathbf{1})=\mathbf{P}(\boldsymbol{n})+\mathbf{3 n}+\mathbf{1}$ for $\boldsymbol{n} \geq \mathbf{2}$. Prove by induction that $\mathbf{P}(n)=\left(\mathbf{3} \boldsymbol{n}^{2}-\mathbf{n}\right) / \mathbf{2}$.
13. Find the Egyptian fraction expansion for 5/26.
14. The hexagonal numbers are given by $\mathbf{H}(2)=6$ and $\mathbf{H}(n+1)=\mathbf{H}(n)+4 n+1$ for $n \geq 2$. Prove by induction that $\mathbf{H}(n)=2 n^{2}-\mathbf{n}$.
