

**Mathematics 205A**  
**Introduction to Topology — I**  
**Course Notes — Part Two**  
**Revised, Fall 2014**

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