

Correction to Section VI.2

In the second paragraph of the proof of the first theorem, the assertion

$$N_\varepsilon(x_n) \cap \left(\bigcup_{i < n} N_\varepsilon(x_i) \right) = \emptyset$$

does not follow from the preceding discussion, but fortunately all we need is the weaker statement

$$x_n \notin \bigcup_{i < n} N_\varepsilon(x_i).$$

This assertion is enough to guarantee that that $\mathbf{d}(x_p, x_q) \geq \varepsilon$ if $p > q$ (and by symmetry if the inequality is reversed), and since the sequence consists of distinct points whose distances from each other are at least ε , it follows that $\{x_n\}$ has no Cauchy (hence no convergent) subsequence.

No changes are needed in the remainder of the proof.