

## MATHEMATICS 132, WINTER 2021, QUIZ 2

**Directions.** The answers to this quiz are to be submitted to the instructor of your discussion section by **11:59 P.M.** on **Friday, March 5.** Please include your name, student identification number, and discussion section number on the worked out quiz.

1. Suppose that two  $n \times n$  matrices  $A$  and  $B$  are similar. Prove that their adjoints  $A^*$  and  $B^*$  are also similar when the scalars are either real or complex numbers (*i.e.*, the result is true in both cases).
2. Give examples of matrices  $A$  and  $B$  of the same size such that  $\exp(A + B) \neq \exp(A)\exp(B)$ . In fact, there are examples in the  $2 \times 2$  case where the entries are not at all complicated.
3. Suppose that the nilpotent  $5 \times 5$  matrix  $N$  is also an elementary Jordan matrix. Show that  $N$  is similar to its adjoint  $N^*$ .

Any valid approach to finding the answers is acceptable (but you may be asked to justify a procedure if it is nonstandard). Although you may consult with other students about material related to these problems, the quiz is **NOT** collaborative; the answers you submit must be your own work and no one else's.