

6/26 Quiz Prep

$$A \setminus B = \{x \in A; x \notin B\}$$
$$(A - B)$$

Set containment Proofs

$$\text{Ex 1: } (A \setminus B) \cup (C \setminus B) = (A \cup C) \setminus B$$

1st proof $(A \setminus B) \cup (C \setminus B) \subset (A \cup C) \setminus B$

Let $x \in (A \setminus B) \cup (C \setminus B)$

if $A \setminus B$, $x \in A$ & $x \notin B$ $A \subset A \cup C$ $x \in A \cup C$ & $x \notin B$

if $C \setminus B$, $x \in C$ & $x \notin B$ $C \subset A \cup C$ $x \in A \cup C$ & $x \notin B$

$$\therefore (A \setminus B) \cup (C \setminus B) \subset (A \cup C) \setminus B$$

Universal Quantifier

\forall for all, every, each

Existential quantifier

\exists there exists, for some, for one

Examples

Definition of continuity

For all $\epsilon > 0$, there exists $\delta > 0$ such that, for all $x, c \in \mathbb{R}$ with c fixed, if $|x - c| < \delta$, then

$$|f(x) - f(c)| < \epsilon$$

odd & even integers

odd An integer n is odd if there exists some integer k such that $n = 2k + 1$

$$f(x) = \frac{x^2 - 4x + 4}{(x - 2)^2}$$

$$(x - 2)^2 \geq 0$$

$$x^2 - 2x + 2$$

$$\frac{+2 \pm \sqrt{4 - 8}}{2}$$

$$\frac{\pm \sqrt{-4}}{2} = \frac{2 \pm 2i}{2} = 1 \pm i$$