

Homework 12, due 5/21, 10pm

1. [5pts] Solve the problem for $w(r, \theta)$ in a unit disk

$$\begin{aligned}\Delta w &= 0, & \text{in } 0 < r < 1, \\ w(1, \theta) &= x^2 + y, & \text{on } r = 1.\end{aligned}$$

Find the expression of $w(r, \theta)$ and then express it in terms of x, y .